

# NMR Strukturbestimmung

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# Konformationsdaten aus NMR Messungen

## Konformationsdaten aus NMR Messungen

1. NOEs
2.  $^3J$  skalare Kopplungen
3. H-Brücken
4. Chemische Verschiebungen
5. Residuelle dipolare Kopplungen (RDC)
- ...

## NOE (Nuclear Overhauser Effect)

NMR Daten: Integral  $V$  von NOESY Kreuzsignalen  
Konformationsdaten: obere Schranken für  $^1H$ - $^1H$  Distanzen,  $d$   
Für isoliertes Spinpaar im starren Molekül:

$$V = C/d^6 \quad \text{mit } C = \text{konstant}$$

Eigenschaften:

- nur kurze Distanzen  $< 5 \text{ \AA}$  messbar
- dichtes Netzwerk bzgl. der Sequenz kurz- und langreichweitiger Distanzschranken
- viele  $^1H$  Atome im Molekül  $\rightarrow$  "Spindiffusion"
- interne Bewegungen  $\rightarrow$  nicht-lineare Mittelung
- Bestimmung der Konstanten  $C$ ?
- Überlapp  $\rightarrow$  mehrdeutige Zuordnung, verfälschte Integrale

## NOE Calibration

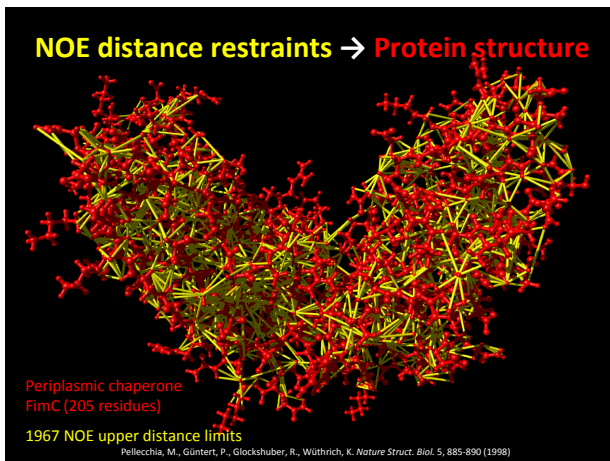
Volume of NOESY cross peak  $\rightarrow V = C / d^6$

"Calibration constant"  $\rightarrow C$

Distance (upper distance bound)  $\rightarrow d$

How to set the calibration constant?

- Known distances (intraresidual or in standard secondary structures)
- Preliminary structure, if available
- User-defined value for the average (median) upper distance limit



## Problems when interpreting NOEs

- Internal motion
- Spin diffusion
- Spectral overlap
- Chemical shift degeneracy
- Time consuming spectral analysis,  
if done manually → **automation**

**NMR resonance assignment  
is like solving a puzzle...**

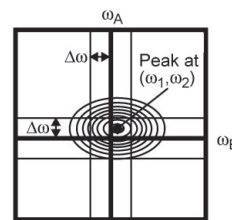
**...with missing pieces  
(incomplete signals)**



**...with additional pieces  
(artifacts)**

**...in the November mist  
(low signal-to-noise,  
line-broadening)**

## Ambiguity of chemical shift based NOE assignment



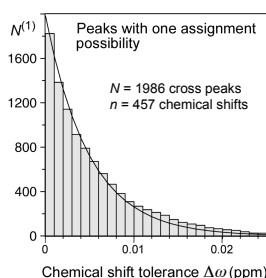
In general, several different  $^1\text{H}$  chemical shifts  $\omega_A, \omega_B$  match the position of a NOESY peak within the experimental uncertainty  $\Delta\omega$ .

→ **Assignment ambiguity**

Manual assignment is very cumbersome!

$$|\omega_1 - \omega_A| < \Delta\omega \quad |\omega_2 - \omega_B| < \Delta\omega$$

## NOEs with a unique chemical shift based assignment



2D NOESY:

$$N^{(1)} \approx N \exp(-4n \Delta\omega / \Delta\Omega)$$

3D NOESY:

$$N^{(1)} \approx N \exp(-2n \Delta\omega / \Delta\Omega)$$

$N^{(1)}$  Number of uniquely assigned peaks

$N$  Number of cross peaks

$n$  Number of chemical shifts

$\Delta\omega$  Chemical shift tolerance

$\Delta\Omega$  Spectrum width

## Ambiguous distance restraints

$$d_{\text{eff}} = \left( \sum_k d_k^{-6} \right)^{-1/6} \leq b$$

$d_k$ : distance for assignment possibility  $k$   
 $\sum$ : sum over all assignment possibilities  
 $b$ : upper distance bound

- Restraint with multiple assignments
  - If one assignment possibility leads to a sufficiently short distance, then the ambiguous distance restraint will be fulfilled.
- The presence of wrong assignment possibilities has no (or little) influence on the structure,  
**as long as the correct assignment possibility is present.**

Nilges et al., *J. Mol. Biol.* 269, 408-422 (1997)

## Properties of ambiguous distance restraints

$$d_{\text{eff}} = \left( \sum_k d_k^{-6} \right)^{-1/6}$$

- $d_{\text{eff}}$  is never longer than any of the individual distances  $d_k$ :  
 $d_{\text{eff}} \leq d_k$  for all  $k$
- $d_{\text{eff}}$  is close to the smallest individual distance:  
 $d_{\text{eff}} \approx d_1$  if  $d_1 \ll d_2, d_3, \dots$
- Examples:  $d_1 = 3 \text{ \AA}, d_2 = 10 \text{ \AA} \rightarrow d_{\text{eff}} = 2.9996 \text{ \AA}$   
 $d_1 = 3 \text{ \AA}, d_2 = \dots = d_{10} = 10 \text{ \AA} \rightarrow d_{\text{eff}} = 2.9967 \text{ \AA}$

## $^3J$ skalare Kopplungen

NMR Daten: Aufspaltung eines Signals

Konformationsdaten: Einschränkungen von Torsionswinkeln,  $\theta$

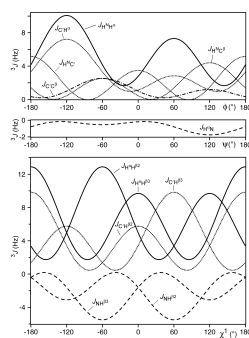
Karplus-Kurve:  $^3J(\theta) = A \cos^2 \theta + B \cos \theta + C$   
mit empirischen Konstanten  $A, B, C$

Zum Beispiel:  $^3J_{\text{HNH}\alpha}(\phi), ^3J_{\text{H}\alpha\text{H}\beta}(\chi^1)$

Eigenschaften:

- Information nur über lokale Konformation
- mehrdeutige Beziehung  $^3J \leftrightarrow \theta$

## $^3J$ scalar couplings



- $^3J(\theta) = A \cos^2 \theta + B \cos \theta + C$
- local information only
- ambiguous relation to torsion angle

## H-Brücken

NMR Daten: langsamer  $^1\text{H} \rightarrow ^2\text{H}$  Austausch + NOEs

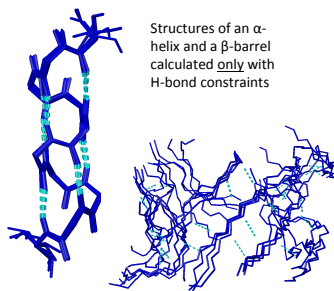
Konformationsdaten: Donor-Akzeptor Distanz

Typische H-Brücken:  $\text{-N-H} \cdots \text{O=C-}$  in regulären Sekundärstrukturen (Helices,  $\beta$ -Blätter)

Eigenschaften:

- Bzgl. Sequenz mittel- und langreichweitig
- Donor (H) identifizierbar
- Akzeptor (O) i. A. nur indirekt bestimmbar (benachbarte NOEs + Annahmen über Sekundärstruktur)

## Impact of hydrogen bond restraints



Structures of an  $\alpha$ -helix and a  $\beta$ -barrel calculated only with H-bond constraints

- Strong impact on structure
- Direct detection of H-bonds by NMR is possible, but not sensitive
- Without identification of acceptor atom  $\approx$  assumption on secondary structure

## Chemische Verschiebungen

NMR Daten: chem. Verschiebungen,  $\delta$

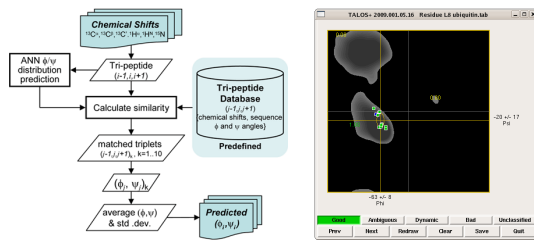
Konformationsdaten:  $(\phi, \psi)$  Torsionswinkelbereiche

Komplexe Beziehung:  $\delta \leftrightarrow (\phi, \psi)$

Eigenschaften:

- einfache Messung
- $(\phi, \psi)$ -Werte aus Datenbank von Proteinen mit bekannter Struktur und chem. Verschiebungen (TALOS)
- Information über lokale Konformation bzw. Sekundärstruktur

### TALOS+: Torsion angle restraints from chemical shifts



#### Reliability of TALOS+ torsion angle predictions:

- TALOS+ makes consistent predictions for, on average, for about 88% of the residues.
- Over all 200 database proteins, about 2.5% of the unambiguous predictions made by TALOS+ were incorrect relative to the corresponding crystal structure. However, a substantial fraction of this 2.5% appears to reflect genuine differences relative to the crystalline state, and the true error rate therefore is believed to be below 2.5%.
- On average, the uncertainty as reported by TALOS+ for the consensus predictions was 12.6° for  $\phi$ , and 12.3° for  $\psi$ .
- The actual RMSD of the "correct" predictions relative to the crystal structures was about 13.5° for  $\phi$ , and 12.9° for  $\psi$ .

### Residuelle dipolare Kopplungen (RDC)

NMR Daten: Zusätzliche Signalaufspaltung bei partieller Molekülausrichtung, z.B.  $^1J_{NH} \rightarrow ^1J_{NH} + D_{NH}$

Konformationsdaten: Orientierung von Bindungen relativ zur Molekülausrichtung

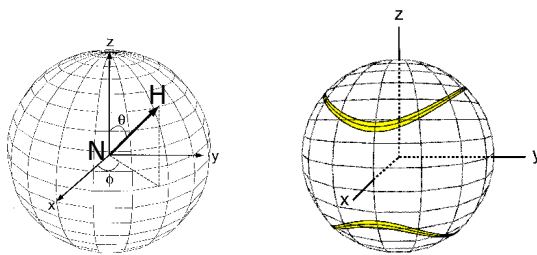
Residuelle dipolare Kopplung:  $D(\theta, \phi) = A [(3\cos^2\theta - 1) + 3/2 R \sin^2\theta \cos 2\phi]$

$A, R$  Amplitude (Betrag) und Rhombizität (Abweichung von Rotationssymmetrie) des Ausrichtungstensors  
 $\theta, \phi$  Richtung der Bindung relativ zum Ausrichtungstensor (Polarkoordinaten)

Eigenschaften:

- Proteinprobe in schwach ausrichtendem Medium (Flüssigkristalle/Bizellen, fadenförmige Phagen, komprimierte Gele)
- Information über globale Konformation, z.B. relative Ausrichtung von Domänen
- Entartung: 1 Messwert  $\rightarrow$  Doppelkegel von Richtungen
- Bestimmung des Ausrichtungstensors ( $A, R$ )?

### Residuelle dipolare Kopplungen



$$D(\theta, \phi) = A [(3\cos^2\theta - 1) + 3/2 R \sin^2\theta \cos 2\phi]$$

### Strukturberechnungs-algorithmen

#### Ist NMR Strukturberechnung möglich?

- Grundsätzlich:
  - NOEs messen nur kurze Distanzen  $< 5 \text{ \AA}$
  - ungenauere obere Schranken
  - Kann damit die globale Struktur eines 30  $\text{\AA}$  langen Proteins bestimmt werden?  
*JA, wenn genügend Daten vorhanden sind.*
- Praktisch:
  - Zielfunktion hat viele lokale Minima
  - Kann eine (fast) optimale Struktur gefunden werden?  
*JA.*

#### Strukturberechnungsalgorithmen

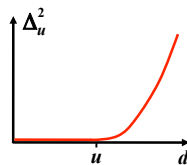
- Frühere Methoden:
  - Interaktiver Modellbau
  - Distanzgeometrie
  - Minimierung einer variablen Zielfunktion
- Simulated annealing:
  - Monte Carlo
  - Moleküldynamiksimulation im kartesischen Raum
  - Moleküldynamiksimulation im Torsionswinkelraum

## CYANA target function

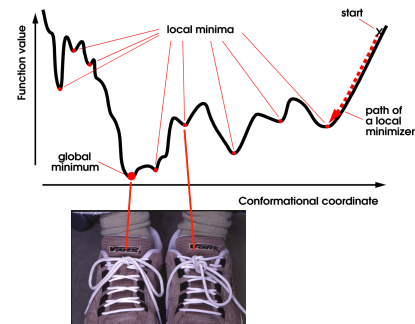
$$T = \sum_{\text{upper distance limits (NOEs)}} \Delta_u^2 + \sum_{\text{lower distance limits (steric)}} \Delta_l^2 + \sum_{\text{torsion angle restraints}} \Delta_a^2 + \dots$$

$\Delta_u, \Delta_l, \Delta_a$ : restraint violations,

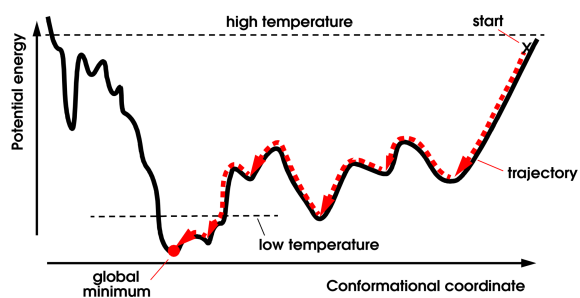
$$\text{e. g., } \Delta_u = \begin{cases} d - u & \text{if } d > u \\ 0 & \text{otherwise} \end{cases}$$



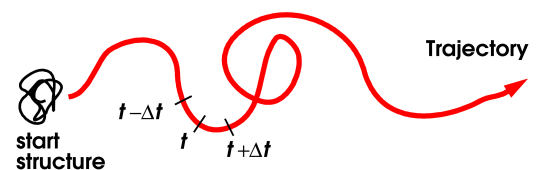
## Target function = potential energy



## Simulated annealing



## Molecular Dynamics Simulation



Numerical integration of classical equations of motion

## Integration of the equations of motion

e.g. "leap-frog" algorithm

$$q(t + \Delta t) = q(t) + \Delta t \dot{q}(t + \Delta t/2) + O(\Delta t^3)$$

$$\dot{q}(t + \Delta t/2) = \dot{q}(t - \Delta t/2) + \Delta t \ddot{q}(t) + O(\Delta t^3)$$

$q$  coordinates (Cartesian or torsional)

$\dot{q} = \frac{dq}{dt}$  velocities

$\ddot{q} = \frac{d^2q}{dt^2}$  accelerations

$\Delta t$  time step

**Atomkoordinaten**  
**Torsionswinkel**

## Strukturbeschreibung

Atomkoordinaten (kartesische Koordinaten):

- 3 Freiheitsgrade pro Atom
- abhängig von der Wahl des Koordinatensystems
- beinhalten auch "unwichtige" Freiheitsgrade
- einfach

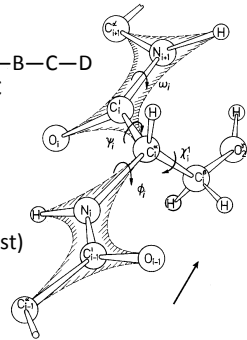
Torsionswinkel (= Diederwinkel, Dihedralwinkel):

- Drehungen um Einfachbindungen
- interne Koordinaten
- essentielle Freiheitsgrade
- Bindungslängen, Bindungswinkel fest
- kompliziertere aber effizientere Algorithmen

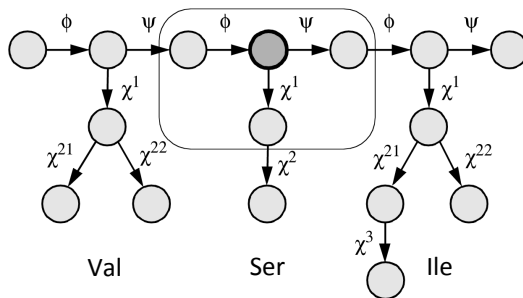
## Torsionswinkel

- Definiert durch 4 Atome: A—B—C—D
- Drehung um Bindung B—C
- Werte von  $-180^\circ$  bis  $+180^\circ$

- Torsionswinkel von AS  $i$ :  
 $\phi_i: C'_{i-1}-N_i-C^\alpha_i-C'_i$   
 $\psi_i: N_i-C^\alpha_i-C'_i-N_{i+1}$   
 $\omega_i: C^\alpha_i-C'_i-N_{i+1}-C^\alpha_{i+1}$  (fest)  
 $\chi^1_i: N_i-C^\alpha_i-C^\beta_i-C'_i$



## Torsionswinkel: Baumstruktur



## MD Simulation im Torsionswinkelraum "Torsionswinkeldynamik"

- Klassische Mechanik
- $N$  Torsionswinkeln als einzige Freiheitsgrade
- Etwa 10 Mal weniger Freiheitsgrade als im kartesischen Raum.
- Feste Bindungslängen und -winkel:  
 → "Einfrieren" der schnellsten Bewegungen  
 → Längere Zeitschritte

Jain, Vaidehi, Rodriguez, *J. Comp. Phys.* 106, 258–268 (1993)  
 Güntert, Mumenthaler, Wüthrich, *J. Mol. Biol.* 273, 283–298 (1997)

## Equations of motion

Cartesian coordinates:  $x_1, \dots, x_N$

$$m_i \ddot{x}_i = - \frac{\partial E_{\text{pot}}}{\partial x_i} \quad (\text{Newton})$$

Generalized coordinates:  $q_1, \dots, q_n$

$$\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{q}_k} \right) - \frac{\partial L}{\partial q_k} = 0 \quad (\text{Lagrange})$$

with  $L = E_{\text{kin}} - E_{\text{pot}}$

## Molecular Dynamics

Cartesian space

$$E_{\text{kin}} = \frac{1}{2} \sum_{i=1}^N m_i \dot{x}_i^2$$

Kinetic energy

diagonal, constant (elements  $m_i$ )

$$\ddot{x}_i = \frac{1}{m_i} \frac{\partial E_{\text{pot}}}{\partial x_i}$$

proportional to  $N$

Torsion angle space

$$E_{\text{kin}} = \frac{1}{2} \sum_{k,l=1}^n M(\theta)_{kl} \dot{\theta}_k \dot{\theta}_l$$

non-diagonal, non-constant,  $n \times n$

Mass matrix  $M$

Accelerations

Computational complexity

$$M(\theta) \ddot{\theta} = C(\theta, \dot{\theta})$$

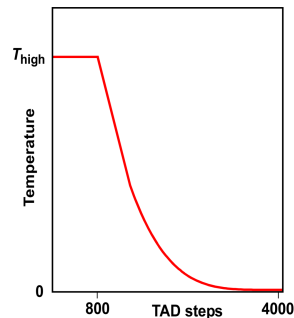
( $n$  linear equations)

solving linear system of equations:  $\sim n^3$

exploiting tree structure of the molecule:  $\sim n$

## Simulated annealing protocol

- Start from random structure
- Use all restraints simultaneously
- Adjustable parameters:
  - start temperature,  $T_{\text{high}}$
  - number of TAD steps



## Temperature control

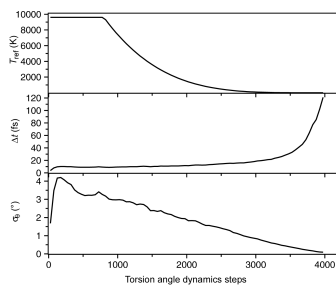
Weak coupling to a heat bath is used to control the temperature:

$$\dot{\theta} \leftarrow \dot{\theta} \sqrt{1 + \frac{T^{\text{ref}} - T}{\tau T}}$$

$\dot{\theta}$  torsional velocities  
 $T$  instantaneous temperature,  $T = \frac{2E_{\text{kin}}}{nk_B}$   
 coupling constant

(Berendsen et al., J. Chem. Phys. 81, 3684–3690, 1984)

## Simulated annealing mit Torsionswinkeldynamik



Temperatur

Zeitschritt

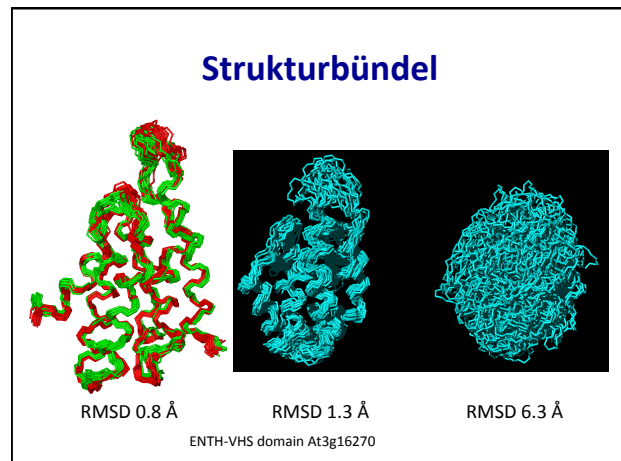
Torsionswinkel-  
änderung

## Strukturbündel RMSDs

## Strukturbündel

- 100 Startstrukturen mit zufälligen Torsionswinkeln
- 100 unabhängige simulated annealing Läufe mit:
  - gleichen experimentellen Daten
  - unterschiedlichen Startstrukturen
- Auswahl der 20 "besten" Strukturen mit den tiefsten Zielfunktionswerten
- Sampling des Konformationsraums?



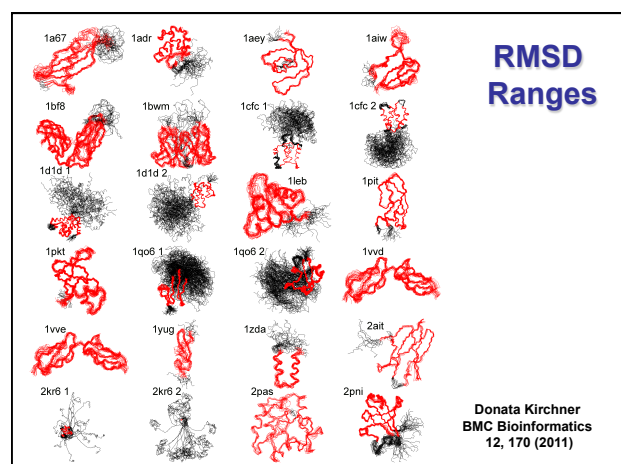
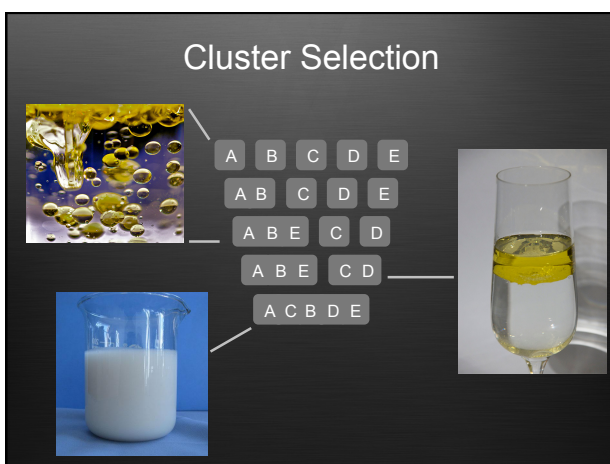
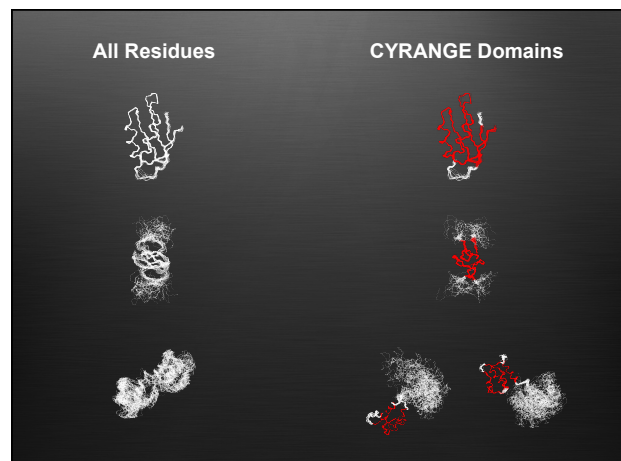


## RMSD (root-mean-square deviation)

- Zwei Strukturen mit  $n$  Atomen und Koordinaten  $\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n$  und  $\mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_n$

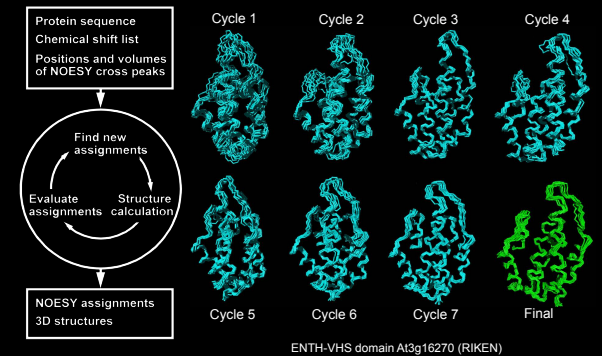
$$RMSD = \min_{R, \mathbf{t}} \sqrt{\frac{1}{n} \sum_{i=1}^n |\tilde{\mathbf{x}}_i - R\tilde{\mathbf{y}}_i - \mathbf{t}|^2}$$

- Minimum über alle Rotationen  $R$  und Translationen  $\mathbf{t} \rightarrow$  optimale Überlagerung



# Automatische NOE Zuordnung

## Automated NOESY assignment and structure calculation with CYANA



## Output overview table

| Cycle                                           | : | 1      | 2     | 3     | 4    | 5    | 6    | 7    | final |
|-------------------------------------------------|---|--------|-------|-------|------|------|------|------|-------|
| <b>Peaks:</b>                                   |   |        |       |       |      |      |      |      |       |
| selected                                        | : | 5439   | 5439  | 5439  | 5439 | 5439 | 5439 | 5439 |       |
| with assignment                                 | : | 5100   | 4806  | 4742  | 4749 | 4712 | 4678 | 4675 |       |
| without assignment                              | : | 339    | 633   | 697   | 690  | 727  | 761  | 764  |       |
| with diagonal assignment                        | : | 12     | 12    | 12    | 12   | 12   | 12   | 12   |       |
| <b>Cross peaks:</b>                             |   |        |       |       |      |      |      |      |       |
| with off-diagonal assignment                    | : | 5088   | 4794  | 4730  | 4737 | 4700 | 4666 | 4663 |       |
| with unique assignment                          | : | 675    | 3591  | 3872  | 3950 | 4115 | 4195 | 4194 |       |
| with short-range assignment $ i-j  \leq 1$      | : | 3295   | 3208  | 3165  | 3154 | 3120 | 3102 | 3089 |       |
| with medium-range assignment $1 <  i-j  \leq 5$ | : | 1020   | 925   | 921   | 914  | 904  | 884  | 893  |       |
| with long-range assignment $ i-j  \geq 5$       | : | 773    | 661   | 644   | 669  | 676  | 680  | 681  |       |
| <b>Upper distance limits:</b>                   |   |        |       |       |      |      |      |      |       |
| total                                           | : | 3786   | 2996  | 2832  | 2789 | 2707 | 2643 | 2683 | 2731  |
| short-range, $ i-j  \leq 1$                     | : | 2007   | 1586  | 1486  | 1440 | 1388 | 1348 | 1273 | 1304  |
| medium-range, $1 <  i-j  \leq 5$                | : | 1220   | 959   | 787   | 775  | 751  | 726  | 760  | 765   |
| long-range, $ i-j  \geq 5$                      | : | 559    | 451   | 559   | 574  | 568  | 569  | 650  | 662   |
| Average assignments/restraint                   | : | 4.81   | 1.73  | 1.27  | 1.25 | 1.18 | 1.14 | 1.00 | 1.00  |
| <b>Average target function value</b>            |   |        |       |       |      |      |      |      |       |
|                                                 | : | 230.84 | 69.79 | 68.20 | 9.22 | 3.99 | 2.98 | 1.70 | 0.43  |
| <b>RMSD (residues 15..130):</b>                 |   |        |       |       |      |      |      |      |       |
| Average backbone RMSD to mean                   | : | 1.34   | 0.97  | 0.57  | 0.67 | 0.68 | 0.60 | 0.53 | 0.53  |
| Average heavy atom RMSD to mean                 | : | 1.76   | 1.44  | 1.09  | 1.19 | 1.20 | 1.07 | 0.98 | 1.01  |

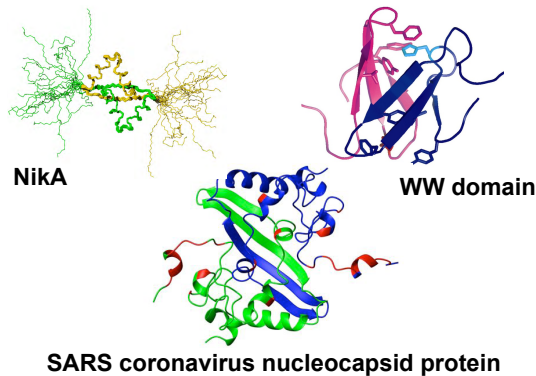
## CYANA Computation Time

- Combined NOE assignment and structure calculation of a 114 amino acid residue protein with the program CYANA:
  - 8 cycles  $\times$  100 conformers = **800 structures**
  - 10000 torsion angle dynamics steps per conformer
- Linux cluster system with Quad-core Intel Xeon E5462 (2.8 GHz, 12 MB cache), 2 GB memory/core

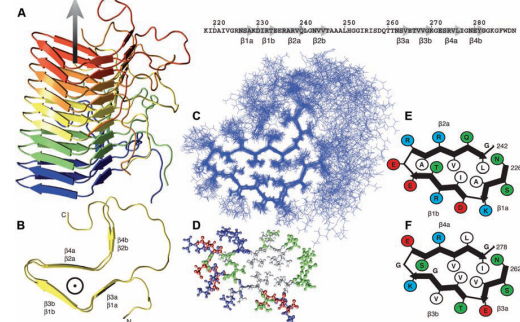
Processors Computation time (s)

|     |     |
|-----|-----|
| 100 | 147 |
| 50  | 217 |
| 25  | 354 |
| 10  | 769 |

## Homodimers



## Structure of HET-s fibrils obtained from solid-state NMR data

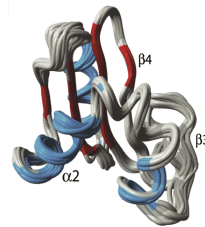


C. Wasmer et al. *Science* 319, 1523-1526 (2008).

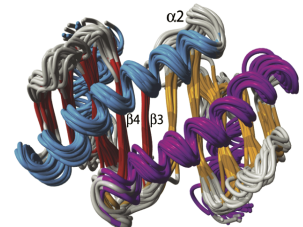
# Strukturanalyse Validierung

## Correct and wrong structure: Dynein light chain 2A

Wrong structure (1TGQ)



Correct structure (1Y4O): Homodimer



Nabuurs, S. B., Spronk, C. A. E. M., Vuister, G. W. & Vriend, G. (2006). Traditional biomolecular structure determination by NMR spectroscopy allows for major errors. *PLoS Comp. Biol.* 2, 71–79.

## Validation principles

Agreement of the three-dimensional structure with

- Experimental data
- Unused experimental data: cross-validation
- Physical principles
- Empirical knowledge about protein structures

Validation of the

- Local structure
- Global structure

Absolute/relative validation:

- Is my structure correct? (“absolute”)
- Is structure A more likely to be correct than structure B? (“relative”)

## X-ray crystallography: *R*-factor

- Measures agreement between measured data (reflections) and 3D structure
- Definition: Relative difference between structure factors,  $F(hkl)$ , that were observed ( $F_{obs}$ ) and back-calculated from the 3D structure ( $F_{calc}$ ):

$$R = \frac{\sum ||F_{obs}| - |F_{calc}||}{\sum |F_{obs}|} \quad \text{with } I_{hkl} \propto |F(hkl)|^2$$

$I_{hkl}$  = intensity of reflection ( $hkl$ )

- Perfect agreement:  $R = 0$
- Good protein X-ray structure:  $R < 0.2$
- Random structure:  $R \approx 0.6$

## X-ray: Free *R*-factor

- Use, say, 90% of the data (reflections) for the structure determination
- Use the remaining 10% to compute the *R* value → “free” *R* value, obtained from independent data
- Detects errors better than conventional *R*-factor
- Each reflection influences whole electron density
- Many reflections → No problem to omit 10% of the reflections from the structure determination

Brünger, A. T. (1992). Free *R* value: a novel statistical quantity for assessing the accuracy of crystal structures. *Nature* 355, 472–475.

## *R*-factor in NMR

- NMR restraints (NOEs) are not raw data but require assignments, calibration, etc.
- Back-calculation of NOEs from 3D structures needs data or assumptions on dynamics and consideration of spin diffusion → “Relaxation matrix calculations”
- Agreement between measured and back-calculated NOESY peak volumes:
  - dominated by strong short-range NOEs
  - absence/presence of a weak (but structurally important!) long-range NOE has negligible influence on the *R*-factor
- Agreement of distances?

## Free R-factor using RDCs

- Use NOE distance restraints to determine structure
- Use residual dipolar couplings to validate
- Quality factor (*R*-factor):

$$Q = \text{rms}(D^{\text{calc}} - D^{\text{obs}}) / \text{rms}(D^{\text{obs}}),$$

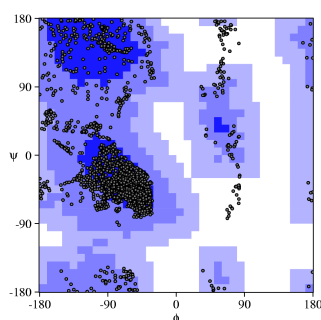
where  $D^{\text{obs}}$  and  $D^{\text{calc}}$  are observed and calculated one-bond dipolar couplings.

Simon, K., Xu, J., Kim, C. & Skrynnikov, N. (2005). Estimating the accuracy of protein structures using residual dipolar couplings. *J. Biomol. NMR* 33, 83-93.

## Validation without experimental data

- Stereochemical quality
- “Normality” of the structure with respect to the existing structures in Protein Data Bank
- Parameters:
  - Bond lengths, bond angles
  - Ramachandran plot
  - Steric overlap (“bumps”)
- Conformational energy
- **3D structure (molecular graphics!)**

## Ramachandran-Plot



Example:  
Each black dot =  
1 residue in 1 conformer

- 73% in most favored regions (dark blue)
- 21% in additionally allowed regions (light blue)
- 4% in generously allowed regions (blue-grey)
- 2% in disallowed regions (white)

(Programm PROCHECK)

## WHAT\_CHECK validation checks

- **Administrative checks:** nomenclature, missing atoms
- **Geometry:** chirality, bond lengths, bond angles, torsion angles (evaluation, Ramachandran plot, omega,  $\chi^1/\chi^2$ ), rings and planarity, proline puckering
- **Structure:** inside/outside profile, bumps, packing, backbone (number of hits, backbone normality, peptide flips), sidechain rotamers
- **Hydrogen bonds:** unsatisfied, flip check, His assignments
- **Summary:** overall Z-scores and RMS Z-scores

$$Z = \frac{X_i - \langle X \rangle}{\sigma(X)} \quad \text{RMS-Z} = \sqrt{\langle Z^2 \rangle}$$

## WHAT\_IF/WHAT\_CHECK output

- Structure Z-scores, positive is better than average:
  - 1st generation packing quality : 0.891
  - 2nd generation packing quality : 1.444
  - Ramachandran plot appearance : -0.105
  - chi-1/chi-2 rotamer normality : -0.431
  - Backbone conformation : 0.551
- RMS Z-scores, should be close to 1.0:
  - Bond lengths : 0.887
  - Bond angles : 1.143
  - Omega angle restraints : 0.437 (tight)
  - Side chain planarity : 0.934
  - Improper dihedral distribution : 1.053
  - B-factor distribution : 3.497 (loose)
  - Inside/Outside distribution : 0.930

Hooft, R. W. W., Vriend, G., Sander, C., Abola, E. E. (1996) Errors in protein structures. *Nature* 381, 272.

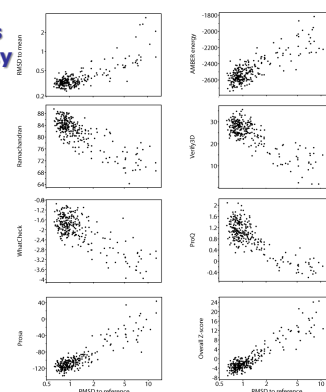
## Correlation between validation parameters and structure accuracy

- 252 ubiquitin structure bundles calculated with CYANA (FLYA)
- Accuracy = RMSD from reference structure
- 7 quality parameters,  $S_i$
- Overall Z-score:

$$Z = \sum_{i=1}^7 \frac{S_i - \bar{S}_i}{\sigma(S_i)}$$

Correlation coefficient 93%

Teppey Ikeya

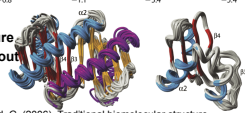


## Quality indicators for correct and wrong structures of DLC2A

Table 1. Average Quality Indicators of the 1Y4O and 1TGQ Structure Ensembles before and after Refinement in Explicit Solvent

| Criteria                                   | Characteristic                                    | 1Y4O (Original) | 1Y4O (Refined) | 1TGQ (Original) | 1TGQ (Refined) |
|--------------------------------------------|---------------------------------------------------|-----------------|----------------|-----------------|----------------|
| Agreement with experimental data           | RMS violation 1Y4O distance restraints (Å)        | 0.0129          | 0.0097         | 0.607           | 0.0284         |
|                                            | Violations >0.5 Å 1Y4O distance restraints        | 0               | 0              | 63              | 0              |
|                                            | RMS violation 1TGQ <sub>dist</sub> restraints (Å) | 12.8            | 12.6           | 0.521           | 0.0231         |
|                                            | Violations >0.5 Å 1TGQ <sub>dist</sub> restraints | 32              | 32             | 4               | 0              |
| RMS violation 1Y4O dihedral restraints (°) | RMS violation 1Y4O dihedral restraints (°)        | 0.497           | 0.336          | 25.0            | 1.59           |
|                                            | Violations >5° 1Y4O dihedral restraints           | 0               | 0              | 34              | 4              |
|                                            | Most favored regions                              | 91.2            | 90.5           | 67.7            | 85.8           |
|                                            | Additionally allowed regions                      | 8.4             | 9.0            | 27.3            | 12.8           |
| PROCHECK validation results*               | Generously allowed regions                        | 0.2             | 0.2            | 4.7             | 0.5            |
|                                            | Disallowed regions                                | 0.2             | 0.3            | 6.2             | 0.9            |
|                                            | Packing quality                                   | -0.4            | 0.1            | -2.1            | -1.5           |
|                                            | Ramachandran plot appearance                      | -3.6            | -3.3           | -6.6            | -4.6           |
| WHAT IF structure Z-scores*                | Z <sub>1/2</sub> rotamer normality                | -0.3            | -0.7           | -5.8            | -3.0           |
|                                            | Backbone conformation                             | -0.8            | -1.1           | -5.4            | -5.4           |

- Better quality indicators for correct structure
- But difficult to detect wrong structure without knowledge of correct structure



Nabuurs, S. B., Spronk, C. A. E. M., Vuister, G. W. & Vriend, G. (2006). Traditional biomolecular structure determination by NMR spectroscopy allows for major errors. *PLoS Comp. Biol.* 2, 71–79.

## CASD-NMR

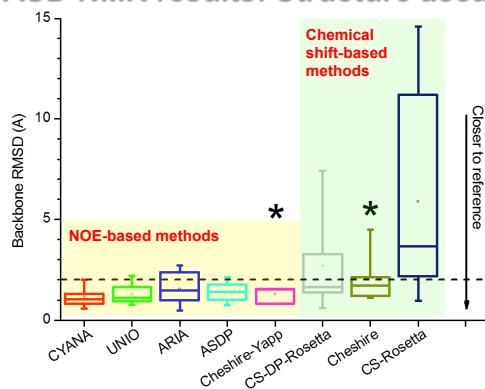
### CASD-NMR: Critical Assessment of Structure Determination by NMR

- Evaluation of current algorithms for automated NOESY assignment and structure calculation
- Blind test (analogous to CASP):
  - NMR data are provided 8 weeks before the release of the structure by the PDB.
  - Structures obtained by different algorithms are collected before the original PDB structure is released.
- Open to anybody for providing data and for calculating structures by automated methods
  - In 1<sup>st</sup> round: 10 protein NMR data sets, 7 algorithms.

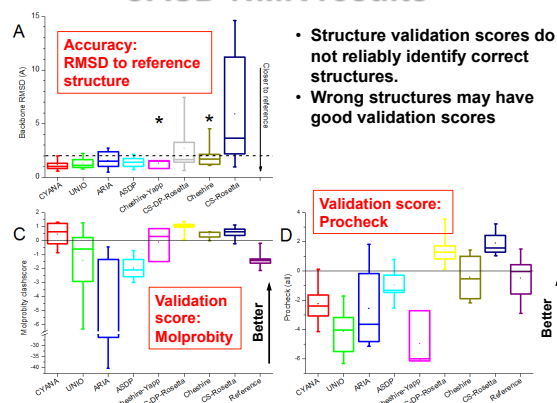
<http://wenmr.eu/wenmr/casd-nmr>

Rosato, A. et al., *Nature Methods* 6, 625–626 (2009)

### CASD-NMR results: Structure accuracy



### CASD-NMR results



### CASD-NMR results: Correlation coefficients between accuracy and validation scores

| Accuracy | Validation scores |          |         |                    |                |                       |
|----------|-------------------|----------|---------|--------------------|----------------|-----------------------|
|          | DP-score          | Verify3D | ProsaII | Procheck (phi-psi) | Procheck (all) | MolProbity Clashscore |
| RMSD     | -0.66             | -0.14    | -0.16   | 0.11               | 0.26           | 0.07                  |

## **Unterlagen zur Vorlesung**

<http://www.bpc.uni-frankfurt.de/guentert/wiki/index.php/Teaching>